







# Unveiling Impacts of Dynamical Effects on the Cataclysmic Variables in Globular Clusters

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# Introduction

## Globular cluster (GC)

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### One of the densest object in the universe

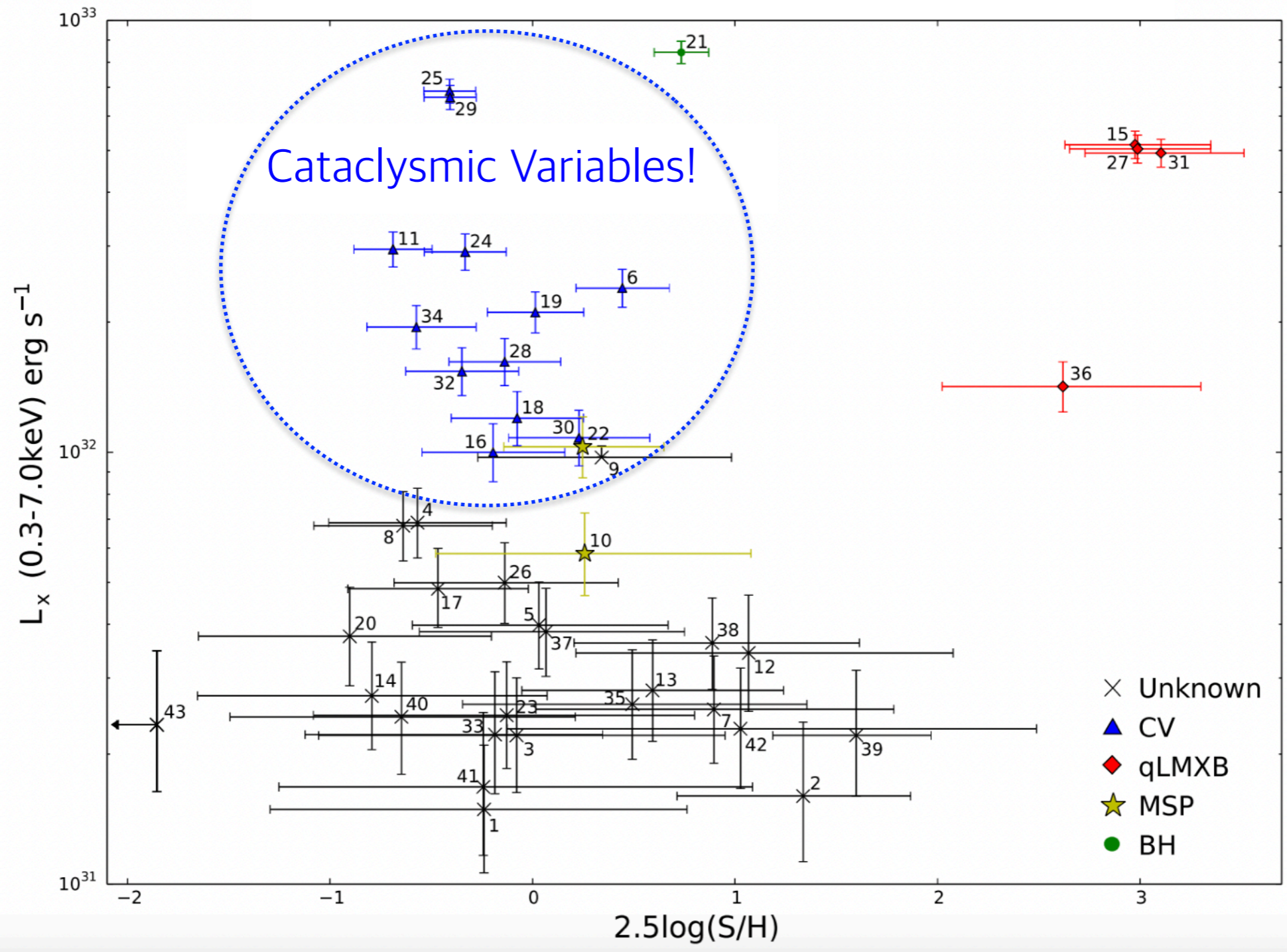
- Strong dynamical interaction (high encounter rate)
- Efficient factory of compact binaries
- ~160 GCs in our galaxy

### Why Globular Cluster

- More exotic phenomena than galactic field
- Resources after launching high resolution telescopes  
(e.g. Hubble space telescope, Chandra X-ray observatory)
- Good window for binary formation episodes
- Already well-known distance

Globular cluster (GC)

# Colour-Magnitude diagram of M62



K. Oh et al (2021)



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# Cataclysmic Variable

## Cataclysmic Variable (CVs)

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### What is CV?

- Binary composed of a White Dwarf (WD) and a Main Sequence (MS) star
- Focus on bright CV (e.g. intermediate polar, polar, magnetic CVs)
- Spectrally hard and bright in X-ray

### Role of CV formation

- GC is good environment for studying formation of CVs
- Interesting formation origin
- Simulation vs Observation



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# MOCCA

MOnte Carlo Cluster simulAtor



## MOnte Carlo Cluster simulAtor (MOCCA)

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### What is MOCCA?

- To perform simulations of a real size star clusters
- N-body simulation (up to  $N=1,000,000$ )
- Few-body interactions
- Includes detailed evolution of each stars
- Good for studying compact binaries dynamics

### How does it work?

- Total 81 models due to the different initial conditions
- Snapshots every 250 Myr
- For the comparison with observation, Present Day Population (PDP), the age around 12 Gyr

## MOnte Carlo Cluster simulAtor (MOCCA)

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### Initial parameters

- Initial seed (200K, 500K, 1M)
- Galactocentric distance (4kpc, 8kpc, 16kpc)
- Half-mass radius (1pc, 2pc, 4pc)
- Initial binary fraction (10%, 20%, 50%)

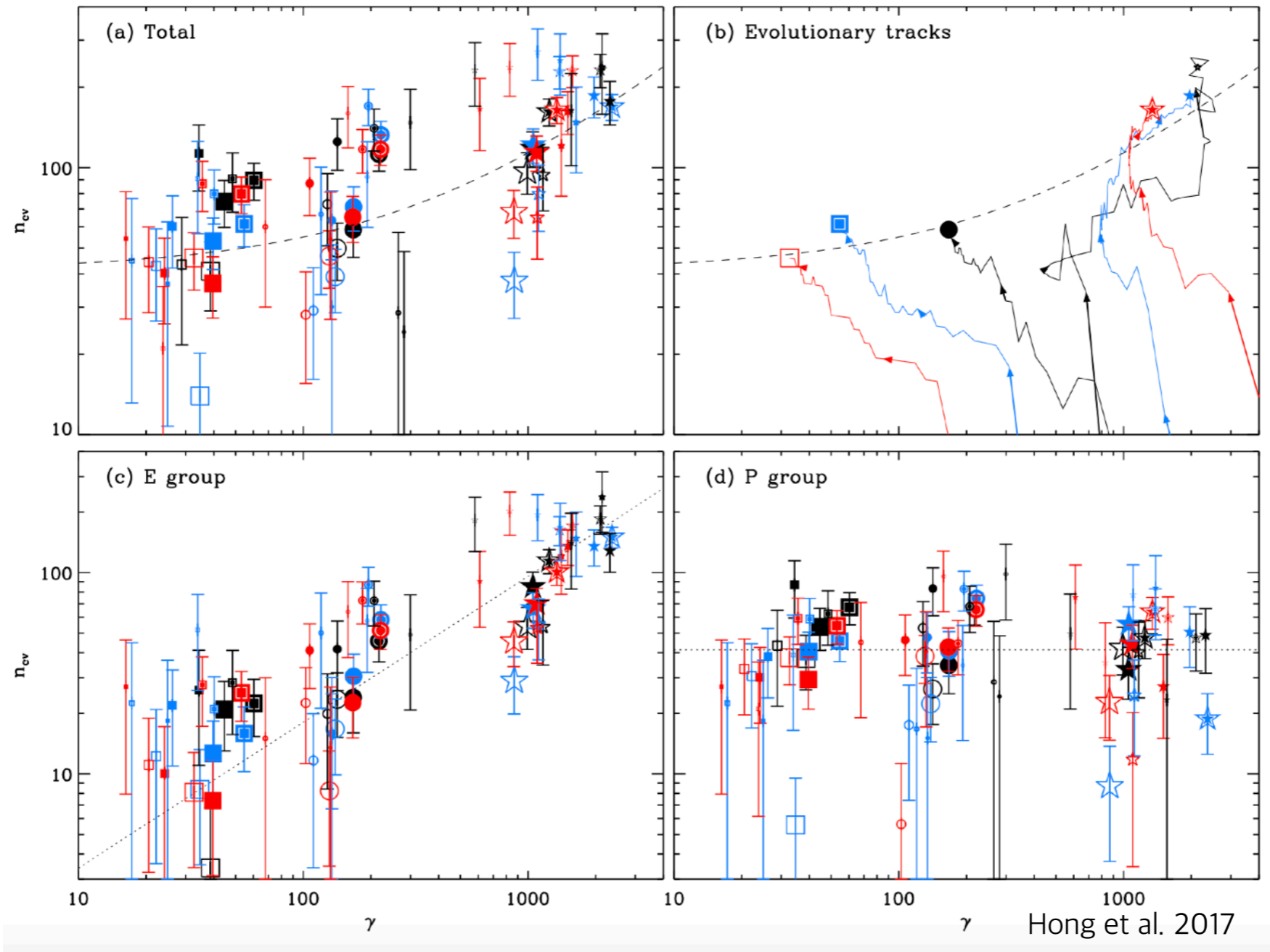


Total 81 GC models

### Previous work by Hong et al. 2017

- Our study can be the extended study which includes X-ray regime
- CV formation mechanism in GC
- Found the correlation between  $N_{CV}$  and encounter rate

# Primordial CVs (P group) & Exchange CVs (E group)



CVs into P group and E group according to their formation origin



Method

## Basic procedure

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### Brief idea before we jump into..

1. CV is comparably easy to classify in X-ray
2. CVs have the large fraction of X-ray emission
3. Can we can derive X-ray luminosity from MOCCA? Yes!
4. Clues for revealing the production dynamics of CVs

$$q = M_1/M_2, \text{ i.e.}$$

$$\frac{R_{L,1}}{a} = \frac{0.49q^{2/3}}{0.6q^{2/3} + \ln(1 + q^{1/3})}$$

### Extracting CVs

- Search for the binaries composed of WD and Main sequence (MS)
- Among those binaries, filtering the binaries which have Roche-lobe overflow
- After sorting out, calculate X-ray luminosity

## X-ray luminosity of CV (simplified)

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### Mass transfer rate

- For the CV with cold/neural and stable and unstable disc (Belloni et al. 2016) :

$$\dot{M}_A = 6.344 \times 10^{-11} \alpha_c^{-0.004} \left( \frac{M_{\text{WD}}}{M_{\odot}} \right)^{-0.88} \times \left( \frac{r}{10^{10} \text{ cm}} \right)^{2.65} M_{\odot} \text{ yr}^{-1}$$

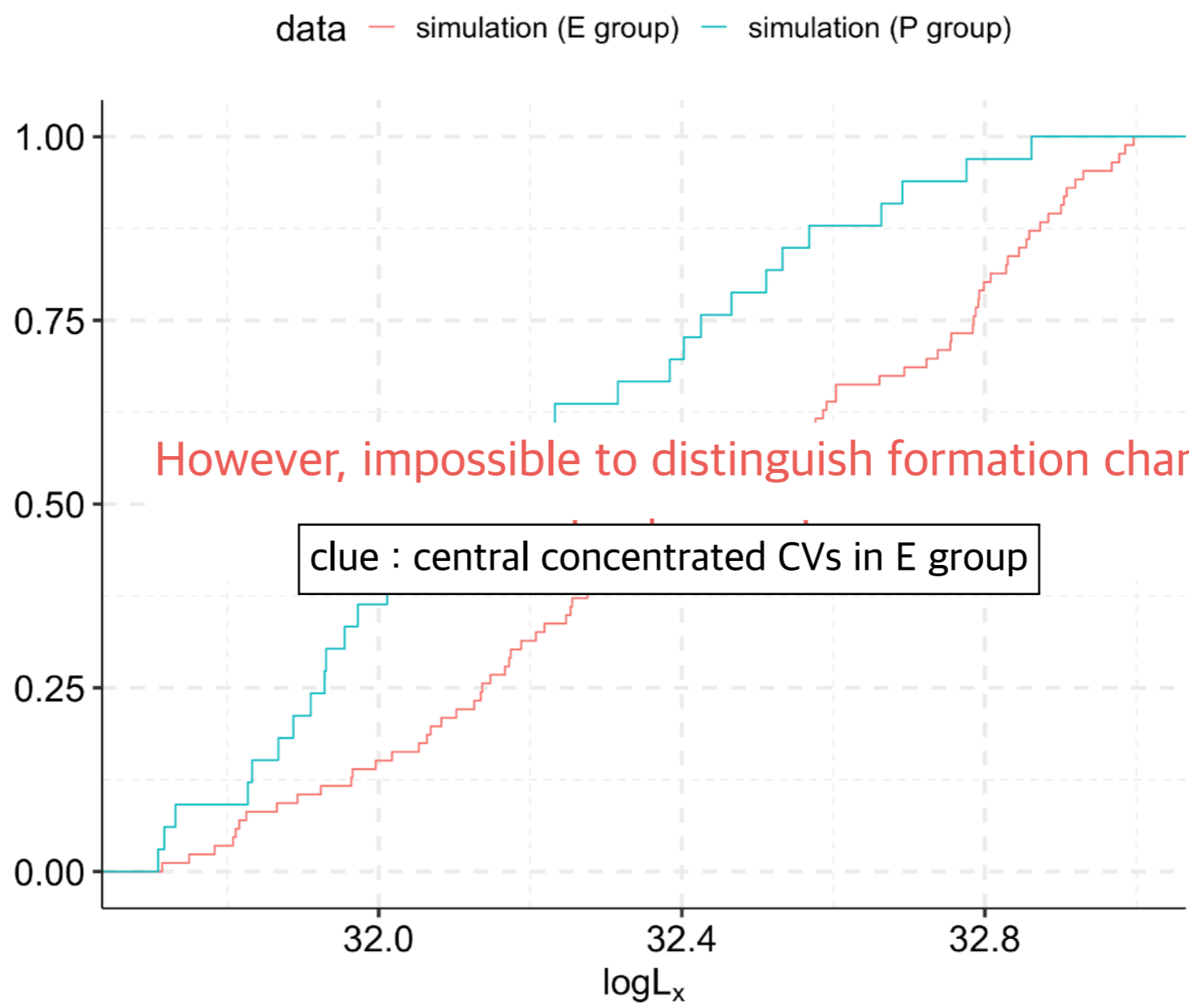
### X-ray luminosity

- Simply adopt slowly rotating WD (Patterson & Raymond, 1985) :

$$L_X = \varepsilon \frac{G M_{\text{WD}} \dot{M}_{\text{dQ}}}{2 R_{\text{WD}}}$$

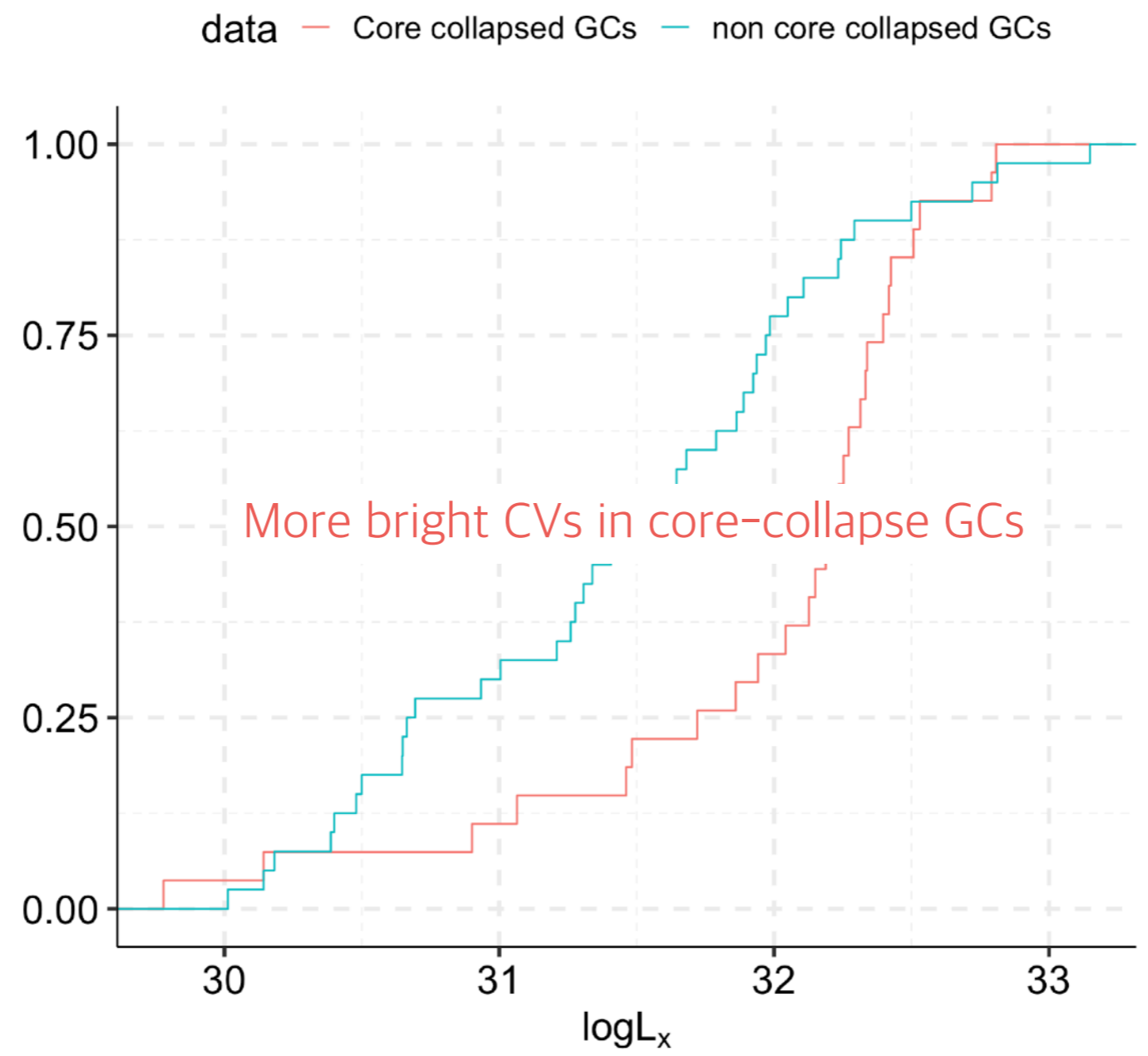
- $\varepsilon = 0.5$ , for the fraction of the X-rays emitted inwards and absorbed by the WD
- $L_X$  cumulative distribution function (CDF) for X-ray distribution for P & E groups

# $L_X$ cumulative distribution function (CDF)



E group and P group distribution in whole 81 GC models at 12 Gyr (PDP)

# $L_x$ cumulative distribution function (CDF)



In the observation, similar phenomena in core-collapsed GCs due to mass segregation effect of the cluster



## Observationally detected CV

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### Observational CV fraction

- CVs in core-collapse GCs dominate comparably higher fraction
- More sample will be adopted in the future

CV domination of $L_x$ in different GCs	
GC name	CV fraction in $L_x^{tot}$
47 TUC	37.27%
Omega-cen	7.21%
NGC6397	84.32%
NGC6752	88.14%

↓  
Core-collapse

: Information for core status from Harris catalog (2010)

- Do bright CVs in core-collapse GCs form via dynamical interaction?

## Core-collapse vs non-core-collapse GC

### Observational CV fraction

- CVs in core-collapse GCs dominate comparably higher fraction
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CV domination of $L_x$ in different GCs	
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↓  
Core-collapse

### How we define core-collapse status in MOCCA GC models?

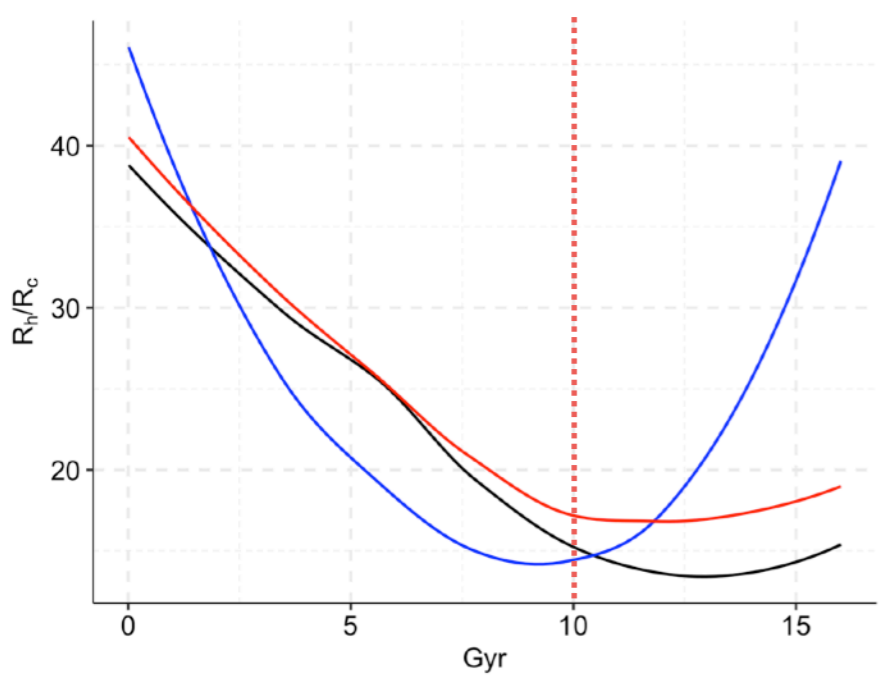
- Tracking the ratio of core-radius & half-mass radius ratio of cluster
- Checking the X-ray luminosity variation
- Number of CVs along the time

# Core-collapse vs non-core-collapse GC

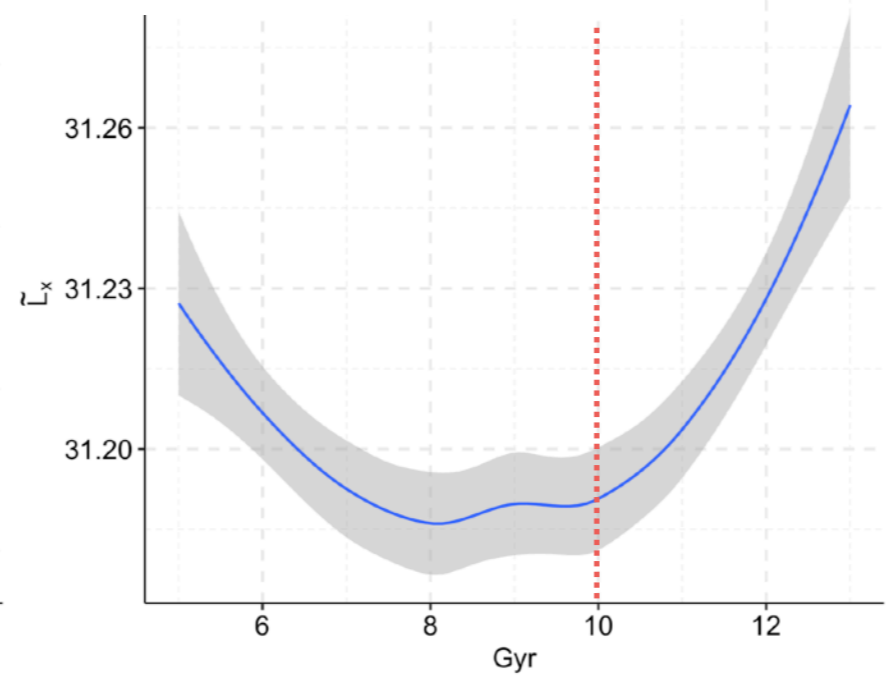
## CV domination of $L_x$ in different GCs

### Observational CV fraction

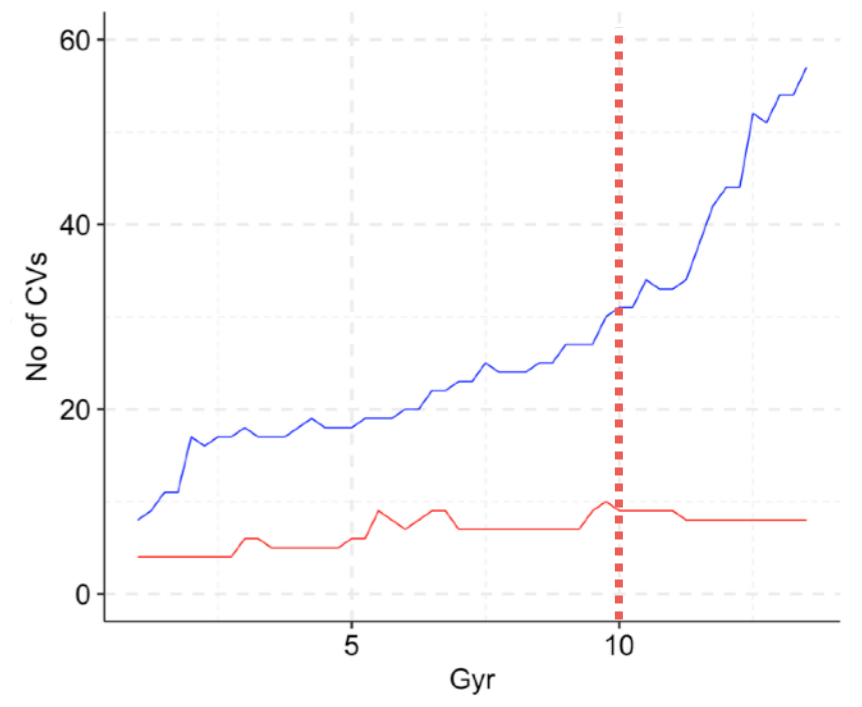
3 simulation models with different initial condition



Core-collapse-like GC model

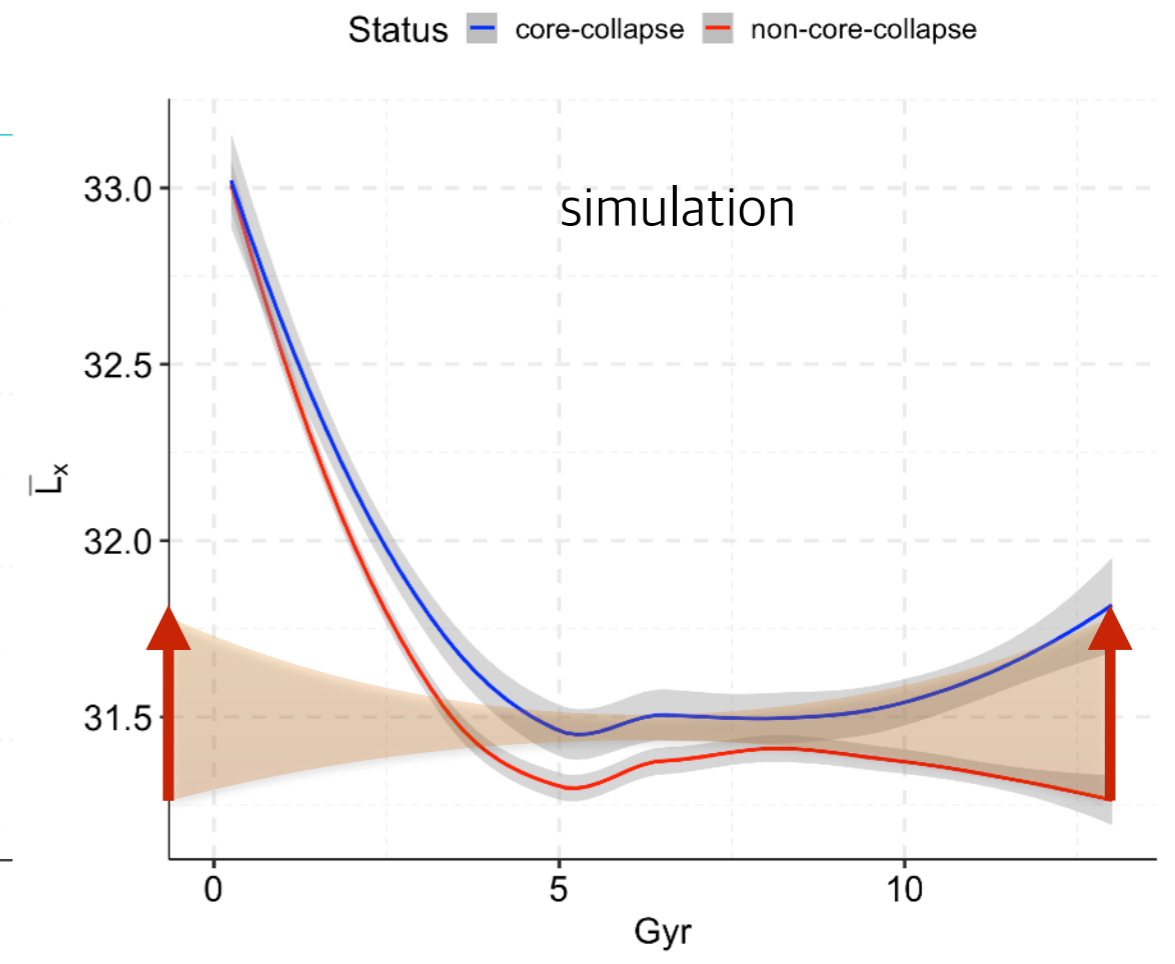
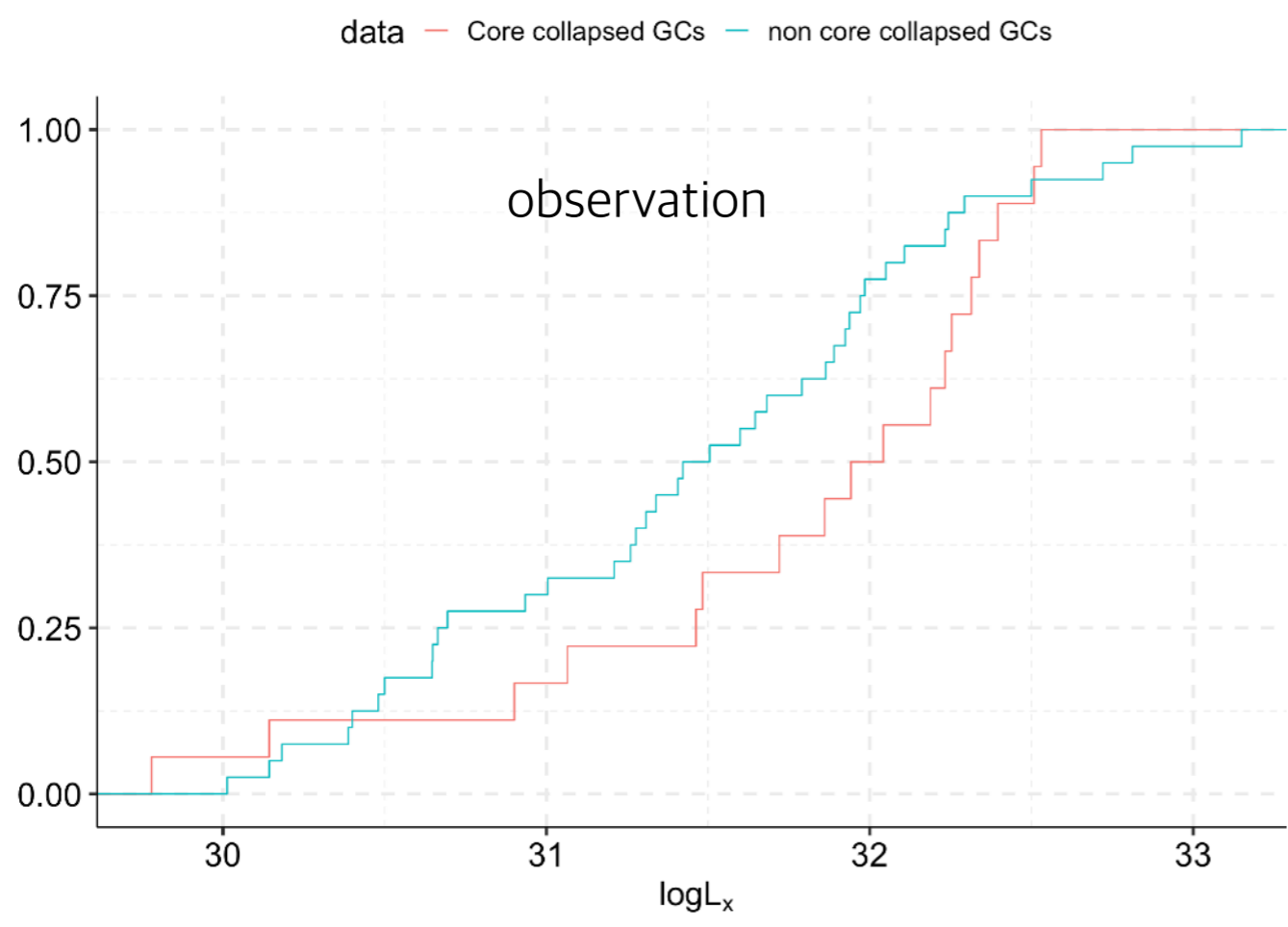


core collapsed GC model — Dynamical — Primordial



In this MOCCA model, core-collapse begins at ~10 Gyr!

# Core-collapse vs non-core-collapse GC



Once we use mean values in both observation and simulation,  
 $\log\Delta L_{X,obs} \sim 0.51$  &  $\log\Delta L_{X,sim} \sim 0.55$

## Further statistical test

### Anderson-Darling test for dominant factors

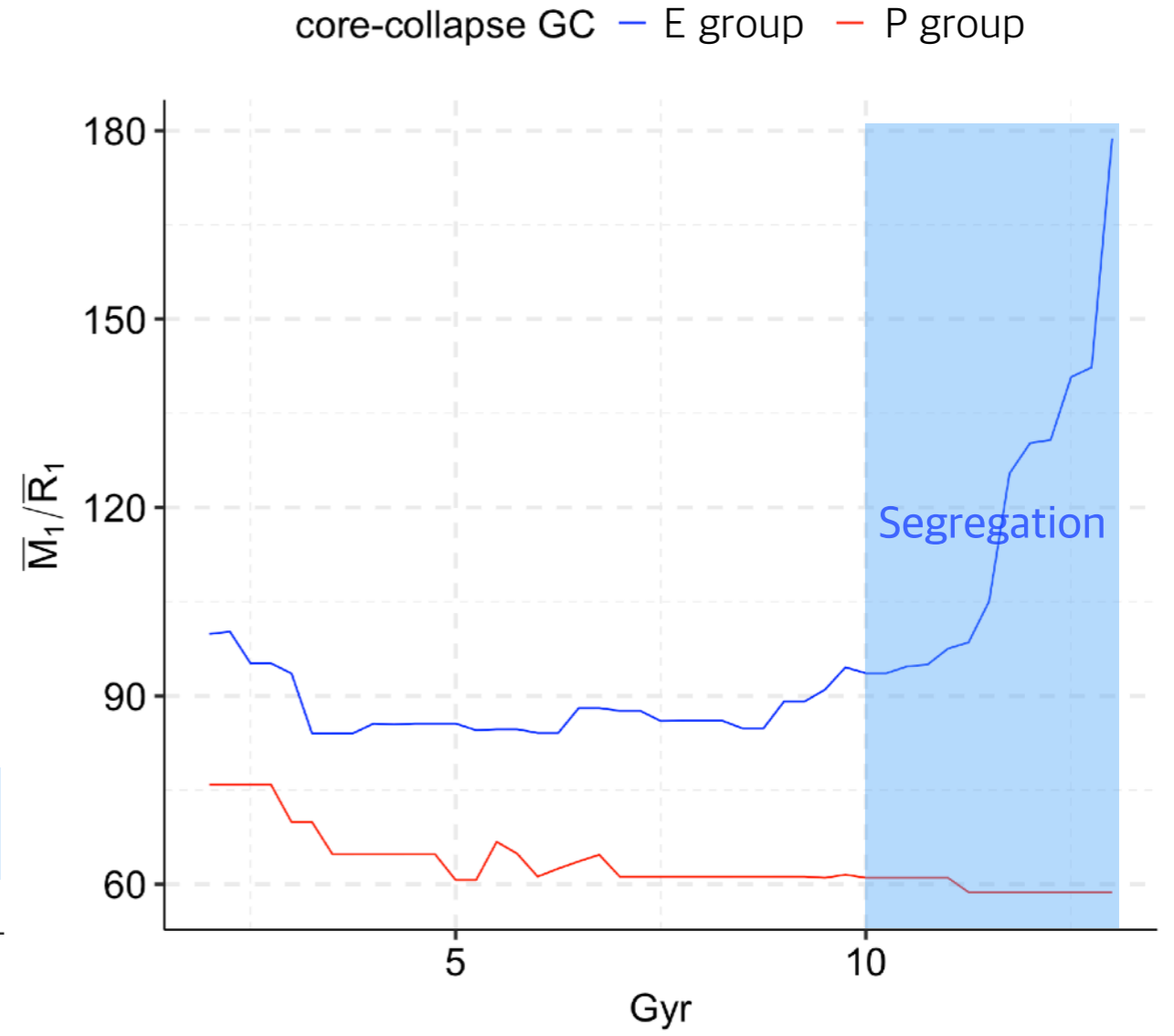
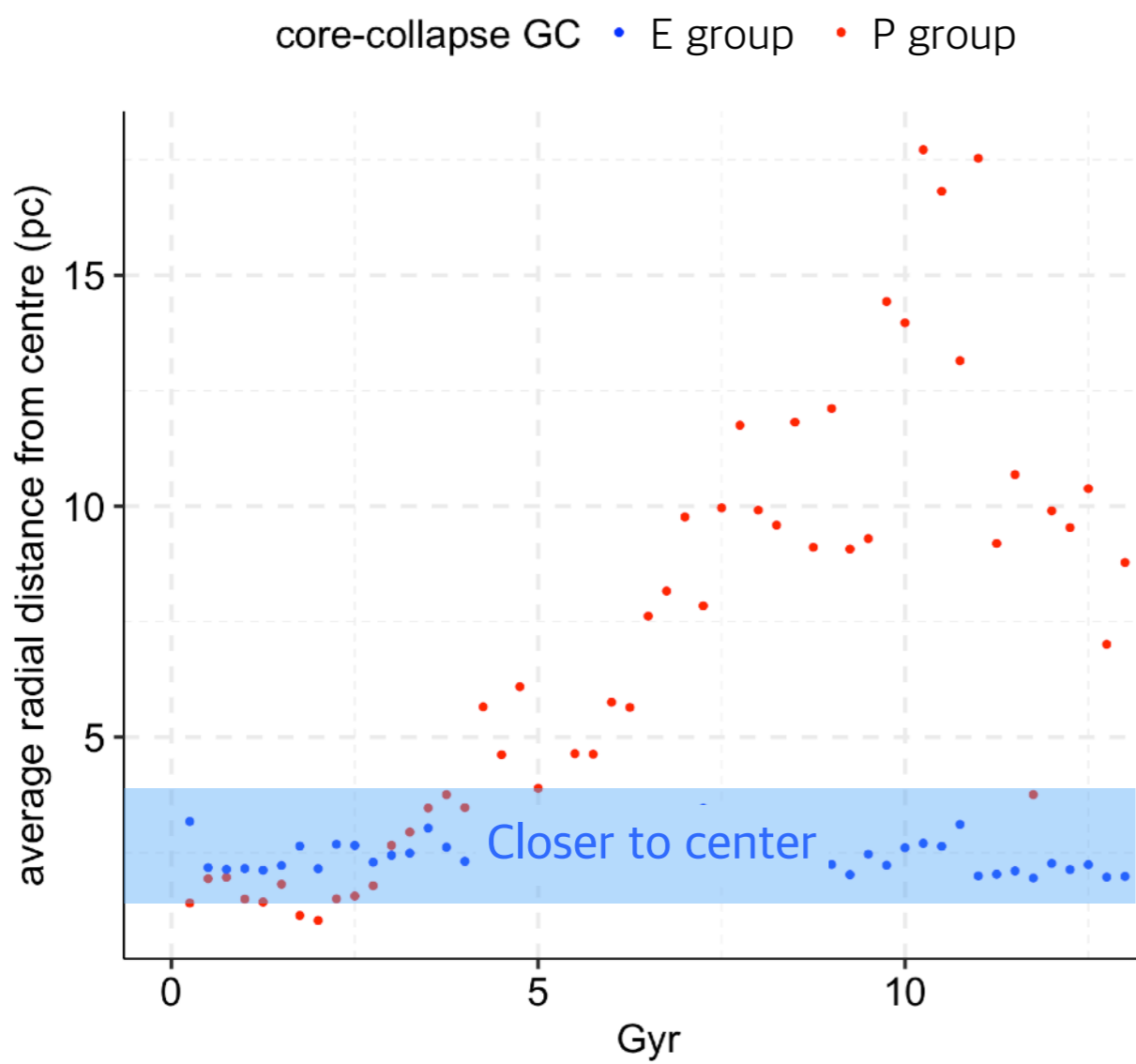
- Which factors are mostly dominate for bright CVs?
- The bigger difference from mass of WD and radius of WD

Anderson-Darling test		
Parameter	AD value	P-value
Semi-major Axis	10.2	7.865e-06
$\log L_x$	13.9	7.453e-08
$\log M_{dot}$	29.7	1.483e-16
Orbital period	29.3	2.423e-16
$M_{ms}$	43.1	6.702e-24
$M_{wd}$	94.1	5.741e-52
$R_{wd}$	94.1	5.741e-52

↓  
**Dominant factors**

P vs E in total 81 models

## Comparison of Dynamical formed CVs & Primordial CVs



- CVs in E group are more concentrated to the core
- According to the method for core-collapse GC, E group CVs increase after core-collapse stage
- It can be the result of 1) mass segregation & 2) increase of core density



# Summary & Future work

## Summary & Future scheme

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### Summary

- Dynamical formed CVs can have dominant fraction of core-collapse GC
- M-R relation can explain deeper gravitational potential & mass segregation effect of GC
- CV population can be a new parameter for considering the evolutionary status of GC
- Not only CVs, the other compact objects would tell us more about GC dynamics

### Future scheme

- LMXB and BH-BH binaries in GC can be new target with MOCCA
- Exotic BH binary such as large eccentricity or tilted rotational axis BH binaries due to dynamical interaction
- Updating MOCCA code for more energetic binary